EECS 665

COMPILER

CONSTRUCTION

Lecture 5
Syntax-Directed Definition

COMPILER

Code Generation

Execution

Runtime Environment

Intermediate Representation

Optimization

SDD

Semantics

Parsing

Lexical Analysis

Syntactic Definiton

Lecture Outline
Syntax-Directed Definition

Recall Syntactic Ambiguity

Assigning Meaning to (Parse) Trees

- Tree translation intuition

- Introduce Syntax-Directed Definition

Tools for SDD

- Bison

Syntax-Directed Definition

Last Time
Review Lecture 4 – Syntactic Ambiguity

Recognizing Context-Free Grammars

- The parser wants a parse tree

Some Challenges in Syntactic Analysis

- Ambiguous Syntax
  - Precedence
  - Associativity

Syntactic Definition

Last Time
Review Lecture 4 – Syntactic Ambiguity

Force precedence constraints

Force associativity constraints

E := E **minus** E
E := E **times** E
E := E **pow** E

E := E **minus** E
 | T
T := T **times** T
 | F
F := F **pow** F
 | G
G := **intlit**

E := E **minus** T
 | T
T := T **times** F
 | F
F := G **pow** F
 | G
G := **intlit**
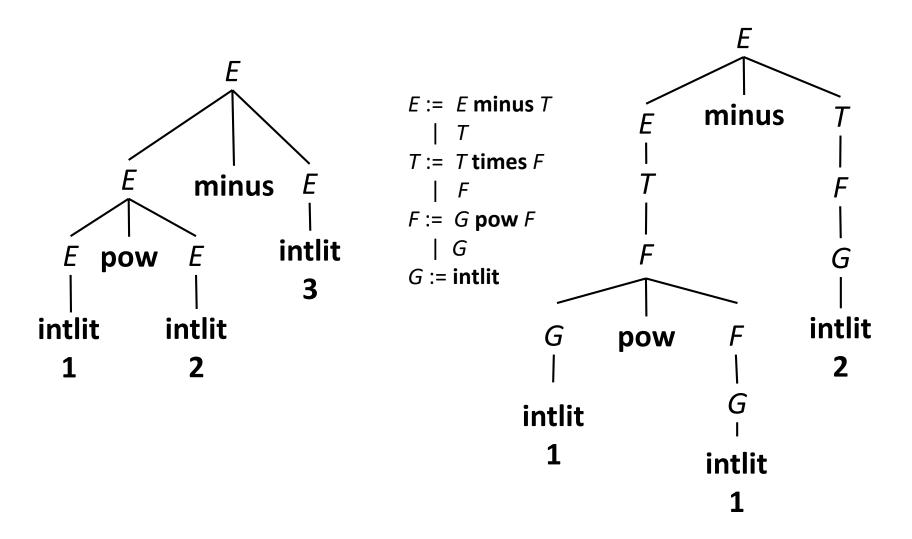
Syntactic Definition

Ensure Bad Exprs are Invalid Syntax
Working with Parse Trees

E := E **minus** T
  | T
T := T **times** F
  | F
F := G **pow** F
  | G
G := **intlit**

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Lecture Outline
Preview Lecture 5 – Syntax-Directed Translation

Recall Syntactic Ambiguity

Assigning Meaning to (Parse) Trees

- Tree translation intuition

- Introduce Syntax-Directed Definition

Tools for SDD

- Bison

Syntax-Directed Definition

Benefits of Parse Trees
Assigning Meaning to Parse Trees

All of the known methods for defining the meaning of computer programs were based on rather intricate algorithms having roughly the same degree of complexity as compilers, or worse. This was in stark contrast to Chomsky's simple and elegant method of syntax definition via context-free grammars. As Dr. Caracciolo said, "How simple to realize [semantic correctness] if you write a procedure. The problem is, however, to find a metalanguage for doing that in a declarative way, not in an operational way" [3].

Benefits of Parse Trees
Assigning Meaning to Parse Trees

- Impose structure on tokens

- Easy to specify

- Easy to process

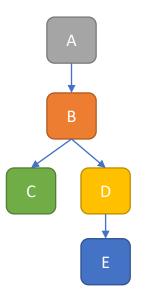**good algorithms
are known**

More generally:
Trees are great data structures
for nesting relationships

Two Ways of Thinking About Trees
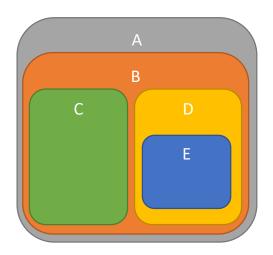## *Working with Trees*

As a type of graph

Compilers use insights from both views

As a type of nesting

Root is a node, children are successors

Work "root-down" vs "leaves-up"
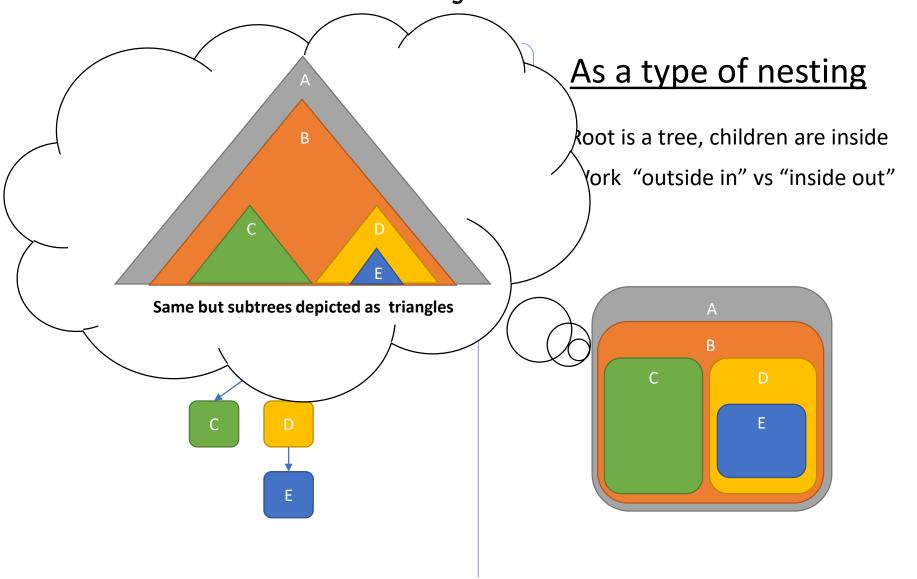
Root is a tree, children are inside

Work "outside in" vs "inside out"

Two Ways of Thinking About Trees

Working with Trees

As a type of nesting

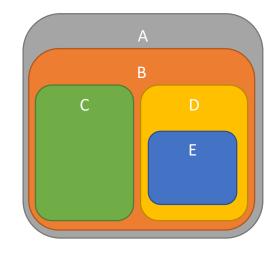Root is a tree, children are inside

Work "outside in" vs "inside out"

A

B

C   D

E

Same but subtrees depicted as triangles

C

D

E

A

B

C   D
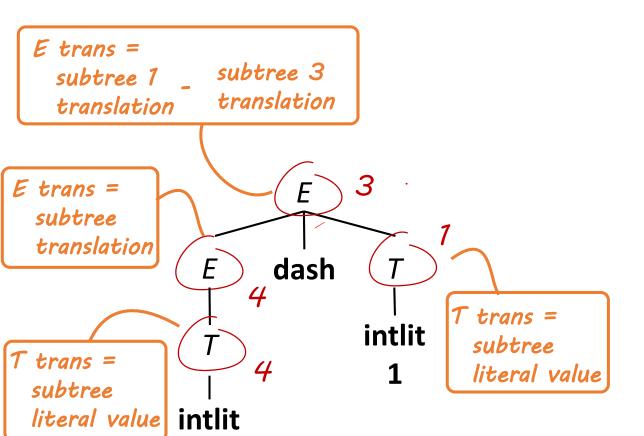
E

Trees as a Nesting
Working with Trees

A = (B)

B = C + D

C = 1

D = (E)

E = 2

also 10, 11]. If we know the meaning of α and the meaning of β, then we know the meanings of such things as $\alpha + \beta$, $\alpha - \beta$, $\alpha \times \beta$, α/β, and (α). Thus the meaning of an arbitrarily large expression can be synthesized in a straightforward way by recursively building up the meanings of its subexpressions.

Assigning Meaning to Subtrees
Processing Parse Trees

Goal: Translation is the value of the expression

Assign a ***translation*** for each node / subtree

E trans = subtree 1 translation - subtree 3 translation

E trans = subtree translation

T trans = subtree literal value

E

dash

T 1

T 4

intlit 1

T trans = subtree literal value

intlit 4

3

4

Grammar:
$E ::= E$ **dash** T
$\quad\quad | \; T$
$T \; ::=$ **intlit**
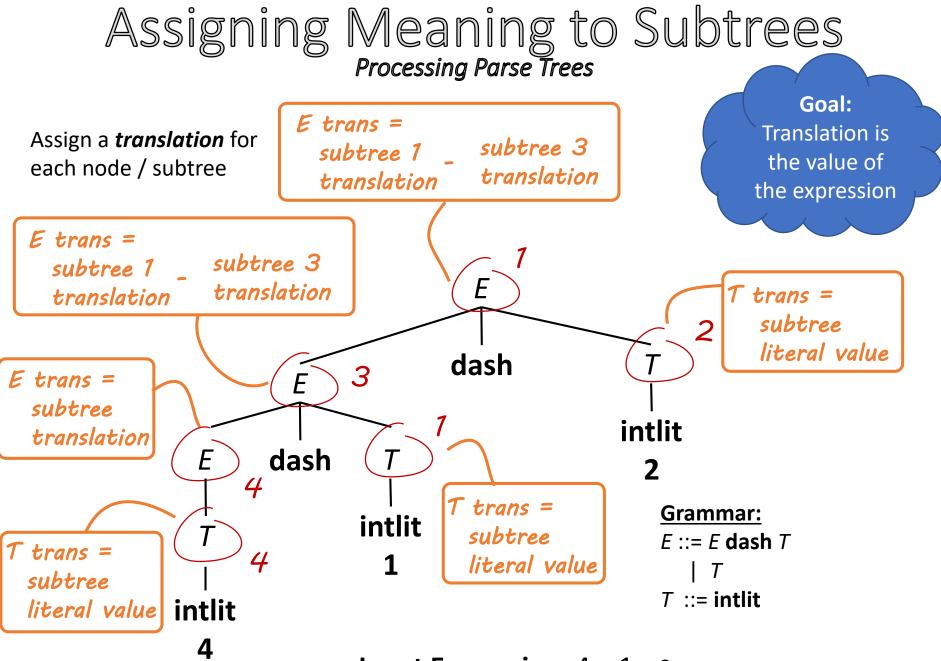
Input Expression: $4 - 1$

Assigning Meaning to Subtrees
Processing Parse Trees

Assign a ***translation*** for each node / subtree

E trans =
subtree 1 translation − subtree 3 translation

Goal: Translation is the value of the expression

T trans = subtree literal value

Input tree (nodes labeled):

- E **1**
  - E **3**
    - E **4**
      - T **4**
        - intlit **4**
    - dash
    - T **1**
      - intlit **1**
  - dash
  - T **2**
    - intlit **2**

Grammar:
$E ::= E$ **dash** T
$\quad\quad | \ T$
$T ::=$ **intlit**

Input Expression: $4 - 1 - 2$

Assigning Meaning to Subtrees
Processing Parse Trees

Assign a ***translation*** for each node / subtree

E trans = subtree 1 translation − subtree 3 translation

E trans = subtree 1 translation − subtree 3 translation

E trans = subtree translation

T trans = subtree literal value

Goal: Translation is the value of the expression

E 1

dash

T 2

E 3

dash

T 1

E 4

intlit 2

T 4

intlit 1

intlit 4

T trans = subtree literal value

T trans = subtree literal value

Grammar:
E ::= *E* **dash** *T*
    | *T*
T ::= **intlit**

Input Expression: $4 - 1 - 2$

In Summary
Processing Parse Trees

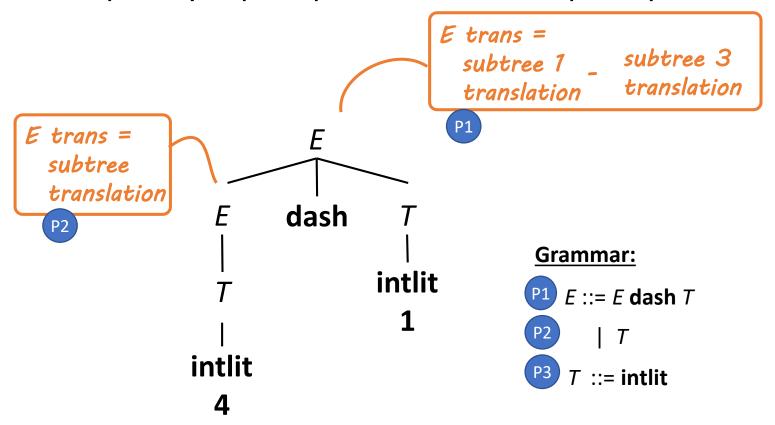- Translation depends on the goal

Goal:
Translation is the value of the expression

Goal:
Translation is the number of operands

Assigning Meaning to Subtrees
Processing Parse Trees

Goal: Translation is the number of operators

E trans = subtree 1 translation + subtree 3 translation + 1

E trans = subtree 1 translation + subtree 3 translation + 1

E trans = subtree translation

T trans = 0

T trans = 0

T trans = 0

Grammar:
$E ::= E$ **dash** T
    $| T$
$T ::=$ **intlit**

Input Expression: $4 - 1 - 2$

Tree Translation Intuition: Summary
Processing Parse Trees

- Translation depends on the goal
- Translation is selected based on the production
- Conceptually, a post-pass over the complete parse tree

E trans = subtree 1 - subtree 3 translation

P1

E trans = subtree translation

P2

E

E   **dash**   T

T   **intlit 1**

intlit 4

Grammar:

P1 $E ::= E$ **dash** T

P2 | T

P3 $T ::=$ **intlit**

Lecture Outline
Preview Lecture 5 – Syntax-Directed Translation

Recall Syntactic Ambiguity

Assigning Meaning to (Parse) Trees

- Tree translation intuition
- Introduce Syntax-Directed Definition

Tools for SDD

- Bison

Syntax-Directed Definition

Semantics of Context-Free Languages

by

DONALD E. KNUTH
California Institute of Technology

ABSTRACT

"Meaning" may be assigned to a string in a context-free language by defining "attributes" of the symbols in a derivation tree for that string. The attributes can be defined by functions associated with each production in the grammar. This paper

Syntax-Directed Definitions
Processing Parse Trees

- Attach translation rules per-production

$X ::= \alpha_1 \ldots \alpha_n$ { *LHS*.trans = *<translation of X that can use translations of $\alpha_1 \ldots \alpha_n$>* }

| $\beta_1 \ldots \beta_n$ { *LHS*.trans = *<translation of X that can use translations of $\beta_1 \ldots \beta_n$>* }

$Y ::= \gamma_1 \ldots \gamma_n$ { *LHS*.trans = *<translation of Y that can use translations of $\gamma_1 \ldots \gamma_n$>*   }

Goal: Translation is the value of the expression

Grammar: **Arithmetic Rules:**

P1 *E* ::= *E* **dash** *T*   { *LHS.trans = E.trans − T.trans* }

P2 | *T*   { *LHS.trans = T.trans* }

P3 *T* ::= **intlit**   { *LHS.trans = **intlit**.value* }

SDD: Example
Processing Parse Trees

P1 rule

E trans =
subtree 1
translation
  –
subtree 3
translation

P1 rule

E trans =
subtree 1
translation
  –
subtree 3
translation

1

E

dash

2

T

P3 rule

T trans =
subtree
literal value

3

E

P2 rule

E trans =
subtree
translation

dash

1

T

P3 rule

T trans =
subtree
literal value

intlit
2

4

E

4

T

P3 rule

T trans =
subtree
literal value

intlit
4

intlit
1

Grammar: **Arithmetic Rules:**

P1 $E ::= E$ **dash** T { $LHS.trans = E.trans - T.trans$ }

P2 | T { $LHS.trans = T.trans$ }

P3 $T ::=$ **intlit**   { $LHS.trans =$ **intlit**$.value$ }

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Lecture Outline
Syntax-Directed Definition

Working with Parse Trees

- Benefits of Parse Trees / Trees in general

- Tree translation intuition

- Syntax-Directed Definition
    - Finer points

Tools for SDD

- Bison

Syntax-Directed Definition

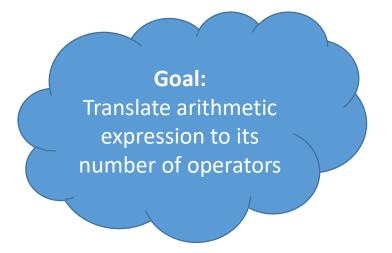# SDD: Parse Tree Processing Multitool
Processing Parse Trees

SDD is a flexible tool for assigning meaning to parse trees

- Useful beyond compilers

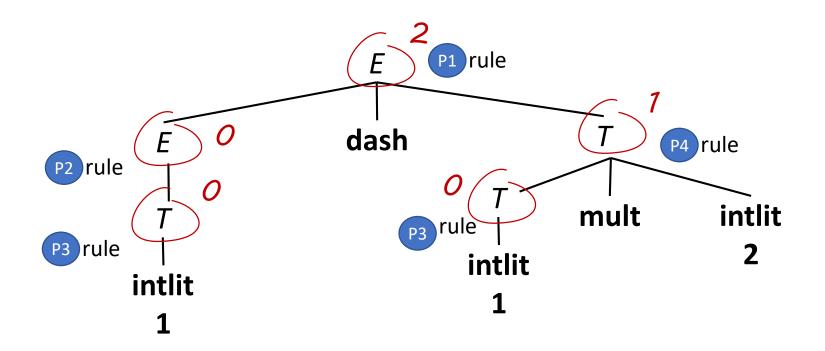- We won't even use the full power of the technique

SDD: A Different Translation Scheme
Processing Parse Trees

- SDD can do more than evaluate expressions

Goal:
Translate arithmetic expression to its number of operators

Grammar:		**Operator Count Rules:**
P1	$E ::= E$ **dash** T	$\{ LHS.trans = E.trans + T.trans + 1\}$
P2	$\| T$	$\{ LHS.trans = T.trans \}$
P3	$T ::=$ **intlit**	$\{ LHS.trans = 0 \}$
P4	$T ::= T$ **mult intlit**	$\{ LHS.trans = T.trans + 1 \}$

SDD: A Different Translation Scheme
Processing Parse Trees

Grammar:

P1 $E ::= E$ **dash** T

P2 | T

P3 $T ::=$ **intlit**

P4 $T ::= T$ **mult intlit**

Operator Count Rules:

{ $LHS.trans = E.trans + T.trans + 1$}

{ $LHS.trans = T.trans$ }

{ $LHS.trans = 0$ }

{ $LHS.trans = T.trans + 1$ }

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SDD: Yet *Another* Translation
Processing Parse Trees
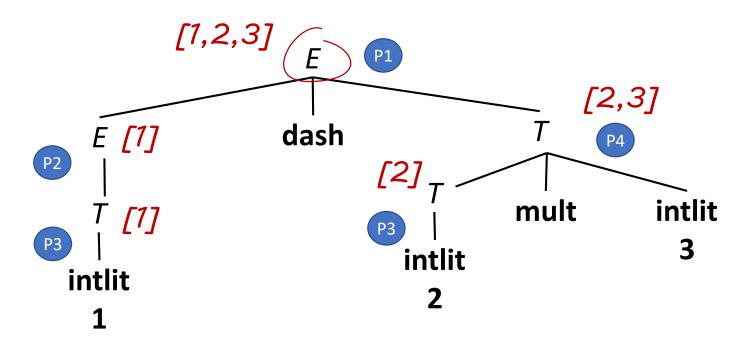
- Myth: SDD translations are always int values

Goal:
Translate arithmetic expression to a list of its int literals

Grammar:

List of integers Rules:

P1 $E ::= E$ **dash** T { $LHS.trans = E$.trans.extend(T.trans) }

P2 $| \ T$ { $LHS.trans = T$.trans }

P3 $T ::=$ **intlit**   { $LHS.trans = [$**intlit.value**$]$ }

P4 $T ::= T$ **mult intlit**   { $LHS.trans = T$.trans.extend([**intlit.value**]) }

SDD: Yet *Another* Translation
Processing Parse Trees

[1,2,3]   E   P1

[1] E   P2   **dash**   T   *[2,3]*   P4

[1] T   P3

[2] T   P3   **mult**   **intlit 3**

intlit 1

intlit 2

Grammar:

P1	$E ::= E$ **dash** T	{ *LHS.trans = E*.trans.extend(*T*.trans) }
P2	| T	{ *LHS.trans = T*.trans }
P3	$T ::=$ **intlit**	{ *LHS.trans =* [**intlit.value**] }
P4	$T ::= T$ **mult intlit**	{ *LHS.trans = T*.trans.extend([**intlit.value**]) }

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SDD: Binary Numbers
Processing Parse Trees

CFG   Rules

  P1: B ::= **0**   *LHS*.trans = ???

  P2: | **1**   *LHS*.trans = ???

  P3: | *B* **0**   *LHS*.trans = ???

  P4: | *B* **1**   *LHS*.trans = ???

Goal:
Translation is the value of the input

Example:
Input string 10110
should be 22
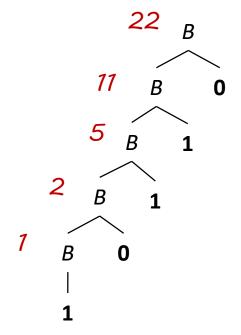
SDD: Binary Numbers
Processing Parse Trees

CFG   Rules

  P1: B ::= **0** LHS.trans = 0

  P2: | **1** LHS.trans = 1

  P3: | B **0** LHS.trans = B_1.trans * 2

  P4: | B **1** LHS.trans = B_1.trans * 2 + 1

Goal:
Translation is the value of the input

22 B

  11 B **0**

    5 B **1**

      2 B **1**

        1 B **0**

          |

          1
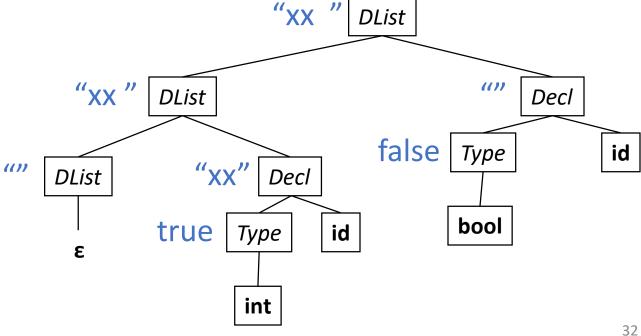
Example:
Input string 10110
should be 22

SDD: Int Declaration List
Processing Parse Trees

CFG

DList ::= **ε**

    | *DList Decl*

Decl ::= *Type* **id ;**

Type ::= **int**

    | **bool**

Rules

LHS.trans = ""

LHS.trans = Decl.trans + " " + $DList_2$.trans

if (*Type*.trans) {*LHS*.trans = **id**.value} else {*Decl*.trans = ""}

LHS.trans = true

LHS.trans = false

Input string
int xx;
bool yy;

Translation is a String of **int** ids only

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BISON: A tool for SDD
Assigning Meaning to Parse Trees

```
15 %union {
16          int intval;
17 }
18
19 %token zero
20 %token one
21
22
23 %type <intval> B
24
25 %%
26
27 S : B        { printf("Value is %d\n", $1); }
28 B :   zero  { $$ = 0; }
29   | one     { $$ = 1; }
30   | B zero  { $$ = $1 * 2 + 0; }
31   | B one   { $$ = $1 * 2 + 1; }
32 ;
33
34 %%
```

Next Time
Lecture Preview

Discuss a use of SDD of particular use to Compilers:

- Translating the parse tree into an *Abstract Syntax Tree*